DISTRIBUTION OF CORRELATED LOGNORMAL RANDOM SUM

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Abstract

Correlated lognormal random sum (CLRS) is random sum, $Z_N = X_1 + X_2 + \dots + X_N$, $N = 0, 1, 2, \dots$, when X_1, X_2, \dots, X_N are correlated and the distribution of X_1, X_2, \dots, X_N given N = l is multivariate lognormal. This paper discusses the approximation distribution for CLRS. The approximation percentile, mean and variance of CLRS are also discussed. Monte Carlo simulation is conducted to investigate the approximations. The simulation results show that the approximation distribution, percentile, mean and variance of CLRS are valid and good approximations.

1. Introduction

The sum of independent random variables also called the *random sum*, $Z_N = X_1 + X_2 + \cdots + X_N$, N = 0, 1, 2, ..., where $Z_N = 0$, has been

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